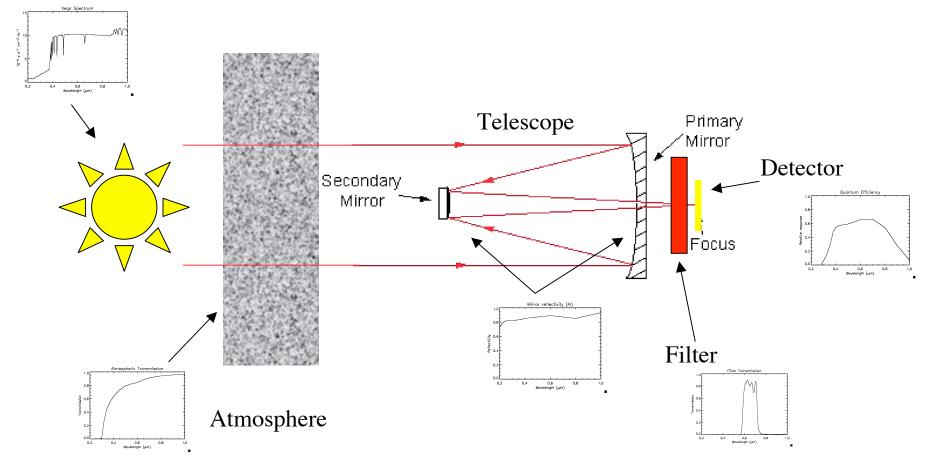
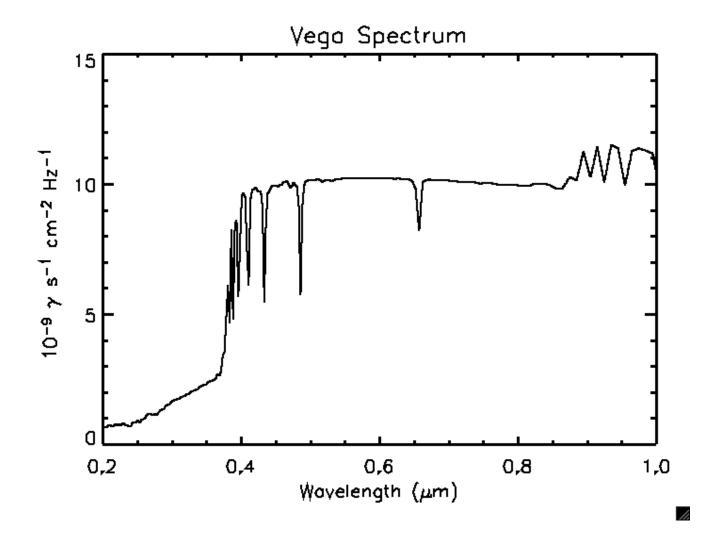
# Starlight, Photoelectrons, & Centroids James R. Graham 10/6/2009

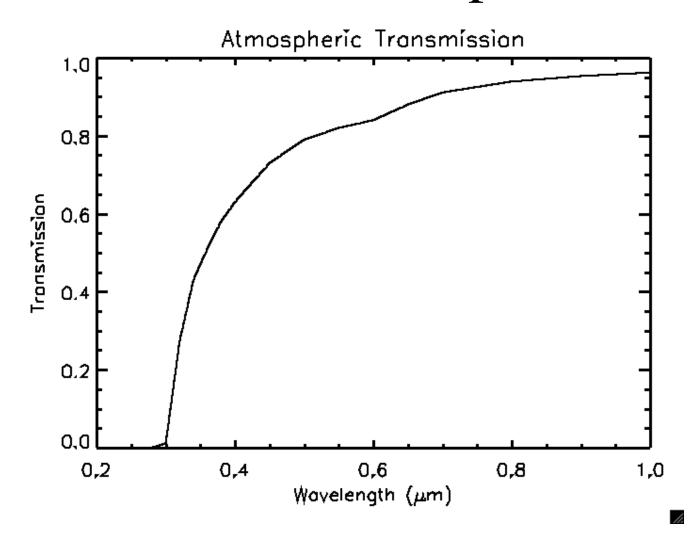
#### Step 1: The Photon Path



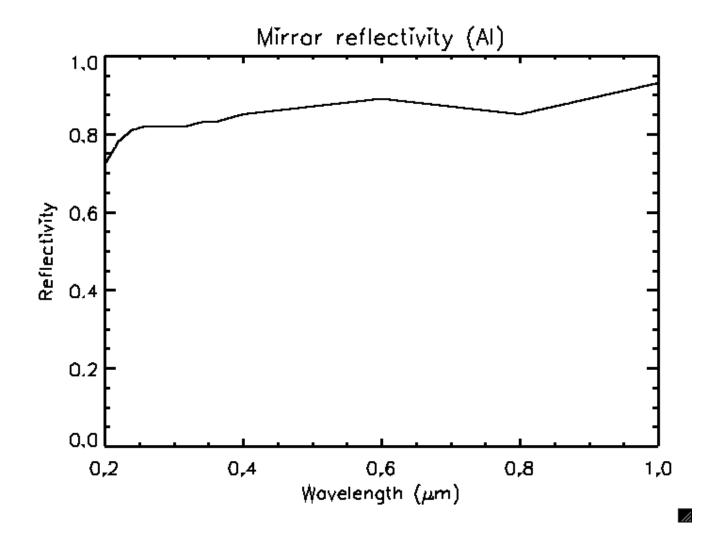




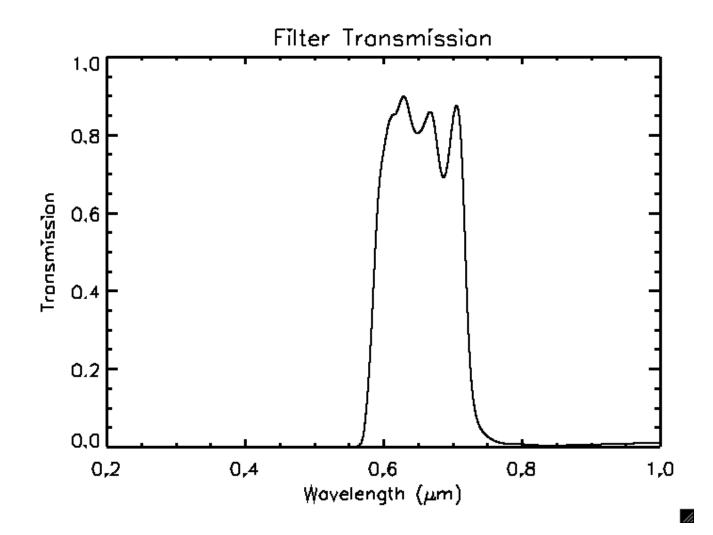
# Scattering & Absorption by the Earth's Atmosphere



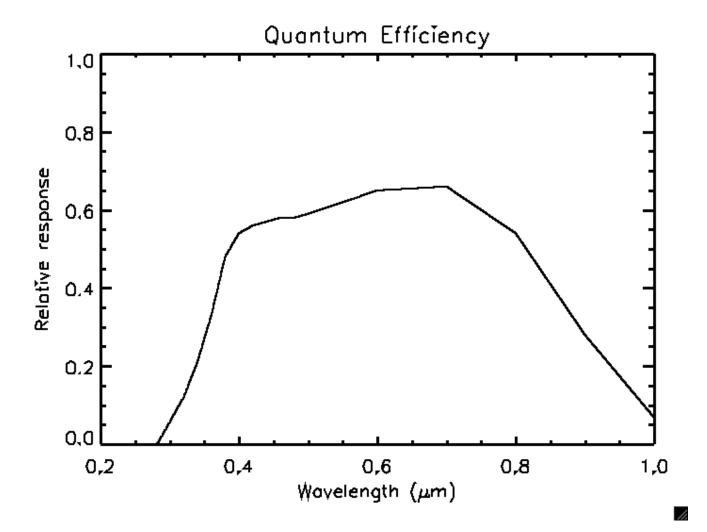


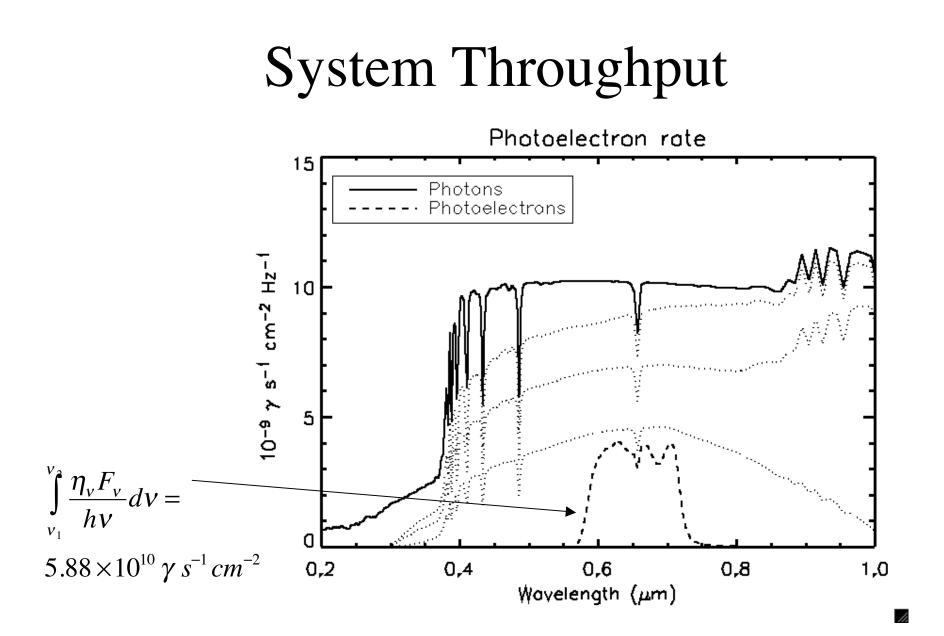


#### Filter Transmission



#### Detector Efficiency





# Step 2: Systematic Errors

- Imaging detectors suffer from a number of errors that must be corrected before the data can be used for photometry
- Goal is to make the DNs from the FITS files proportional to the brightness of the astronomical source

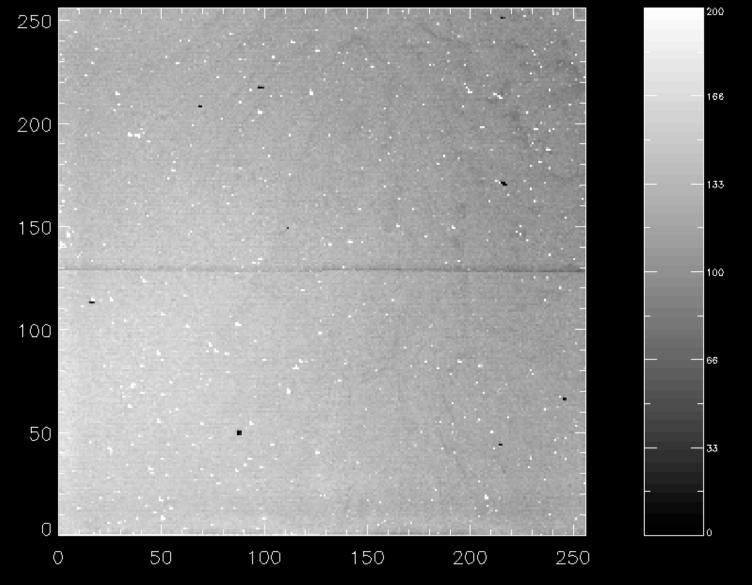
#### Bias & Dark Current

- Even a zero second exposure gives nonzero DN
  - Dark current masquerades as real signal
  - Dark current & bias (constants DC offset) can be removed either by subtracting
    - 1. A dark frame of the same exposure time as the science image—takes care of bias too, or
    - 2. An image of blank sky—takes care of bias & dark, and also subtracts the sky brightness! (can be hard to find blank sky)

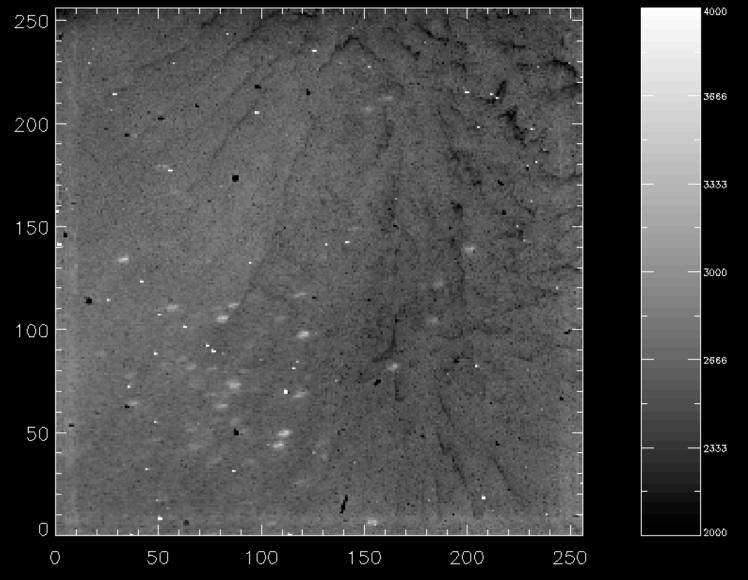
# Relative Pixel Gain a.k.a. Flat Field

- Every pixel in the detector array has a slightly different response to light
  - Some pixels are more efficient than others
- Need to correct for pixel-to-pixel variations by constructing a flat field
  - Make a flat field by observing a uniform source,
     e.g., the twilight sky
  - Divide dark-subtracted images by the flat field

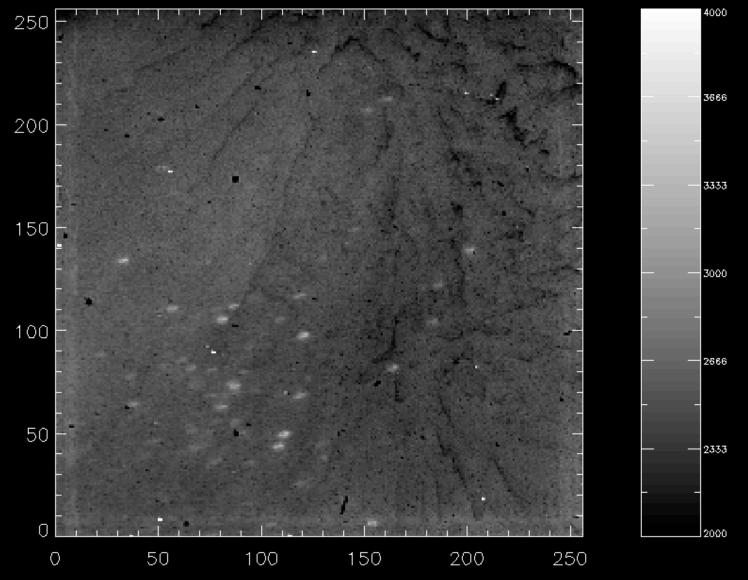
Dark



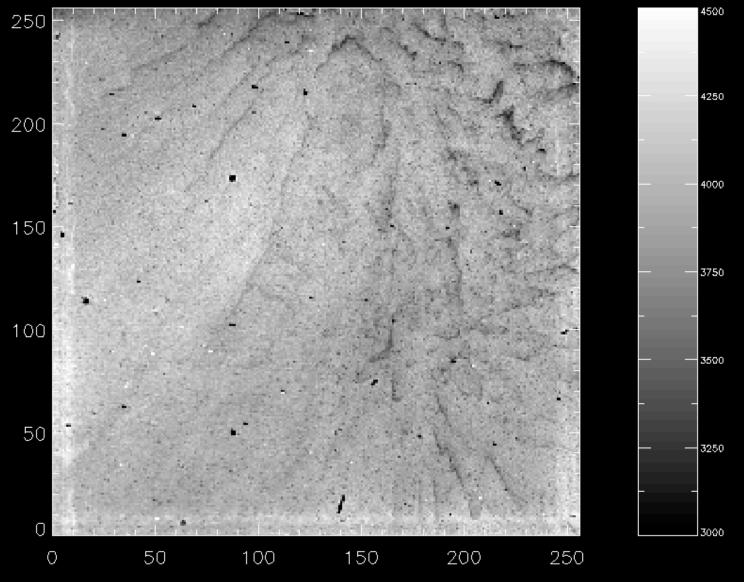
M13 Raw

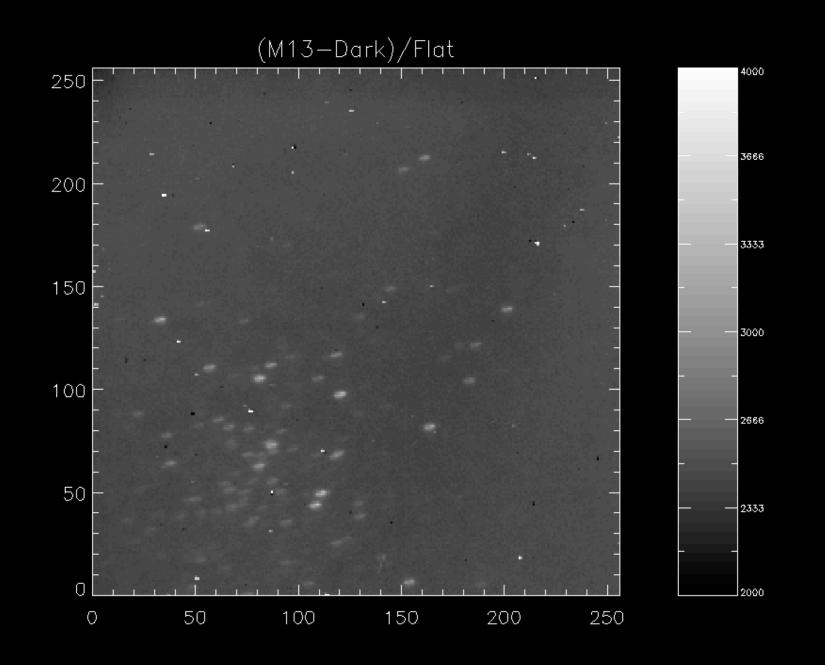


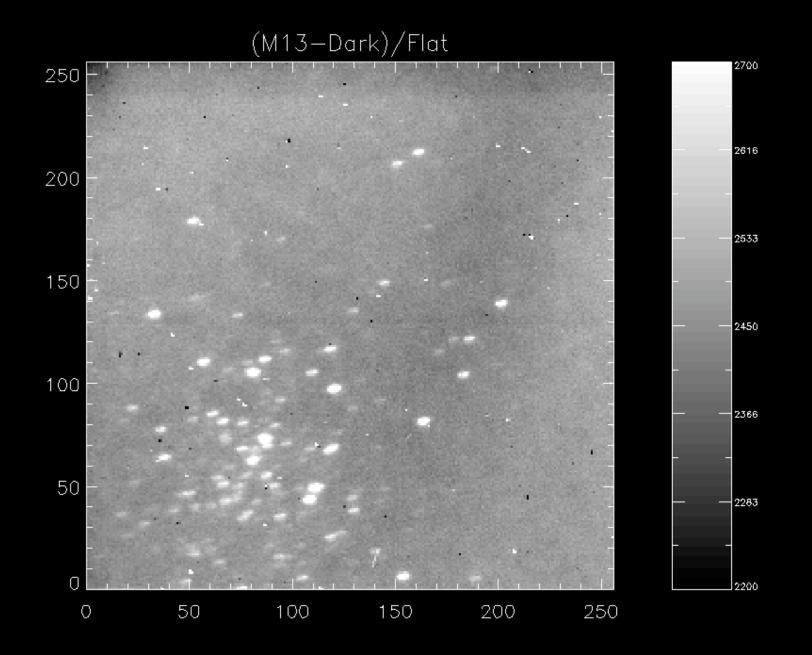
M13-Dark











#### Moments

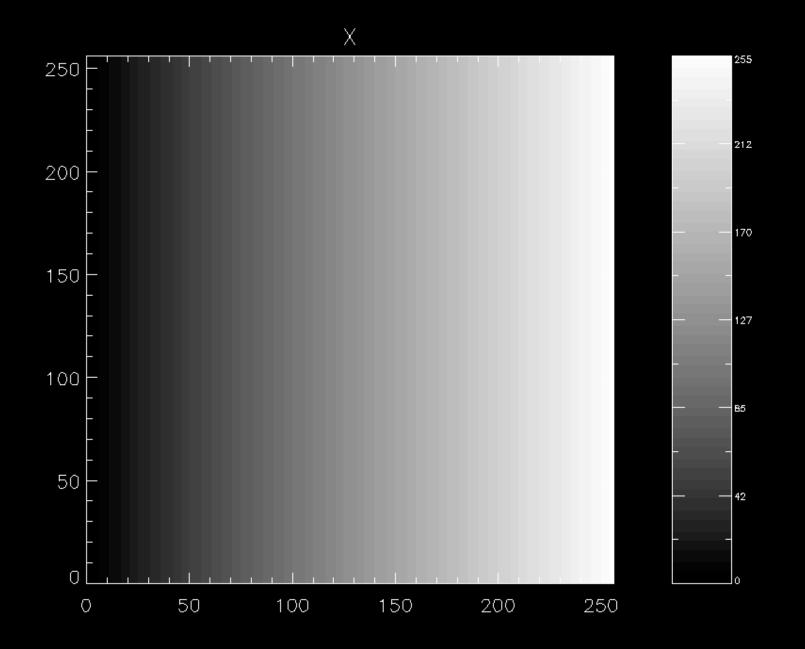
• For each star we can construct moments of its light distribution

– The first moment is

$$\left\langle x\right\rangle = \sum_{i} x_{i} I_{i} / \sum_{i} I_{i}$$

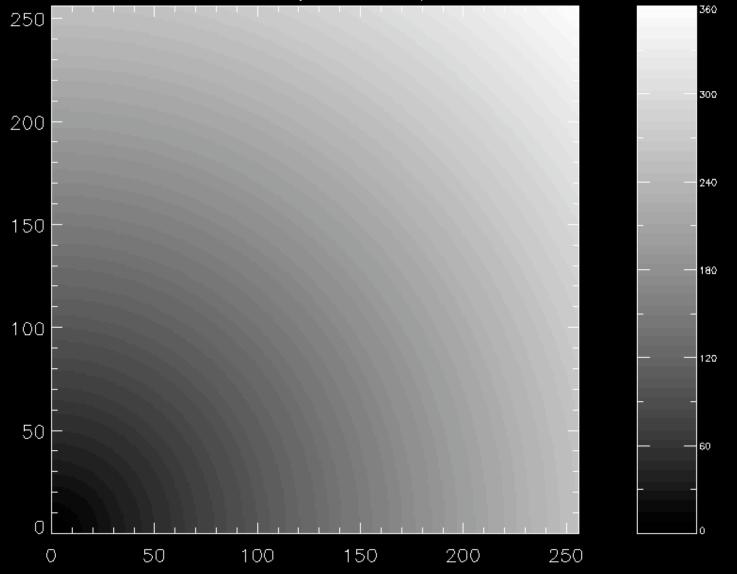
# How Bright is that Star?

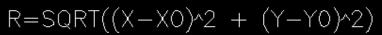
- The light from a star is spread over several pixels
- How do we sum the light to get a measure of the total signal from the star?
  - 1. Identify the location of the star (RDPIX)
  - 2. Select the associated pixels by making a mask
  - 3. Sum up the light (TOTAL)
    - Subtract the sky background if necessary

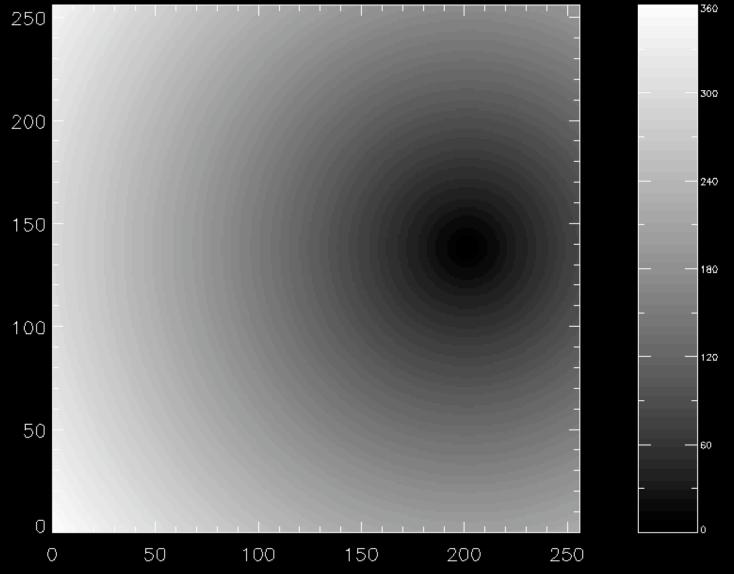


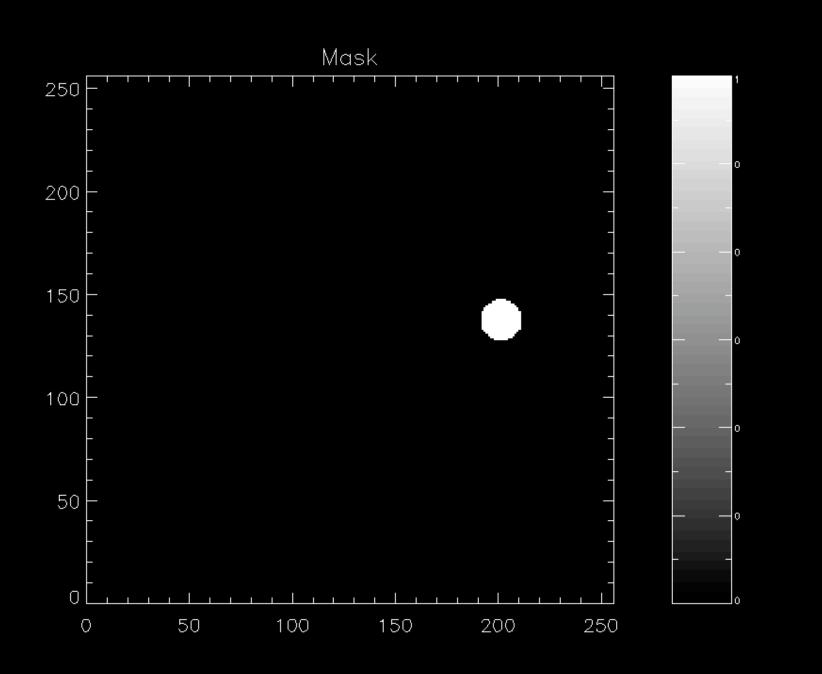
Y - 65 - 42 ١û 

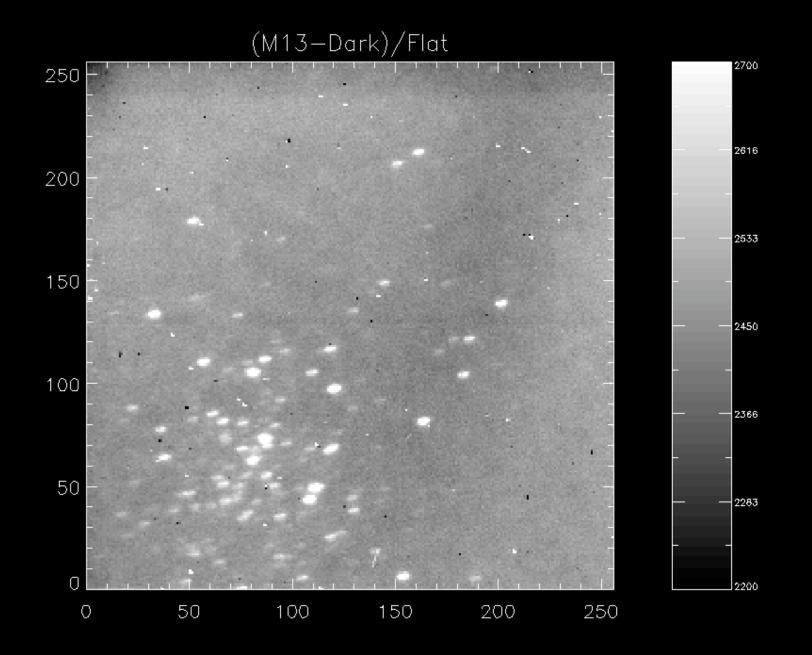
 $R = SQRT(X^2 + Y^2)$ 

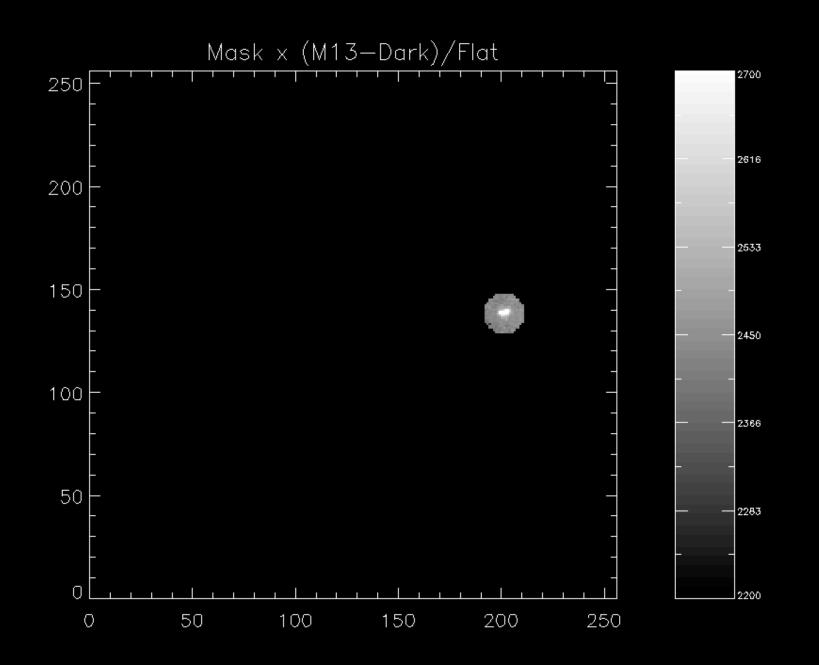


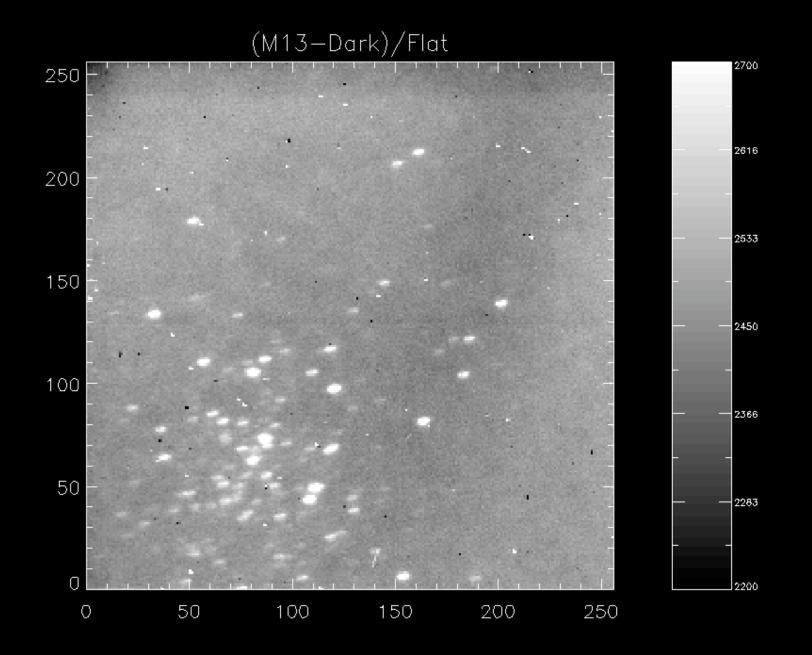


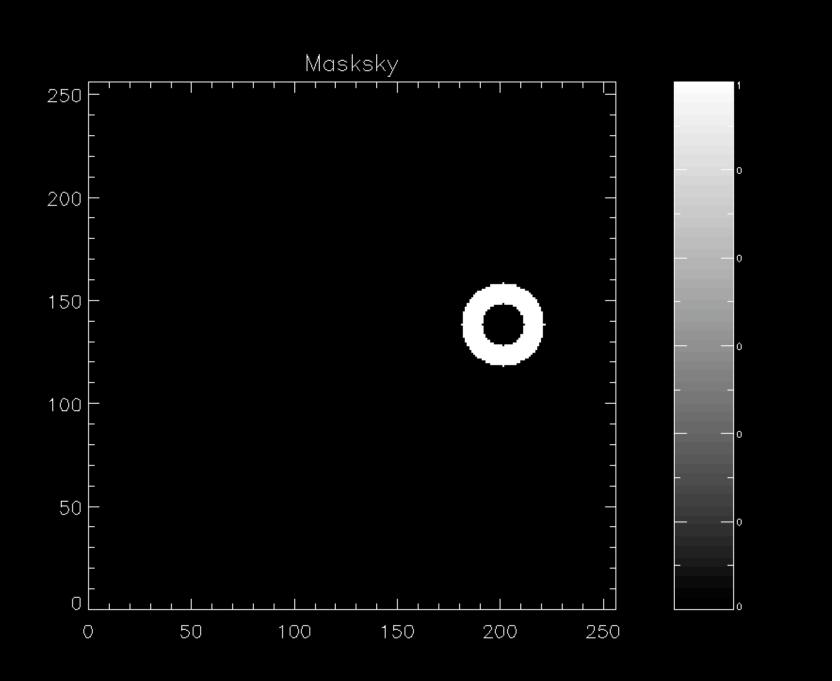


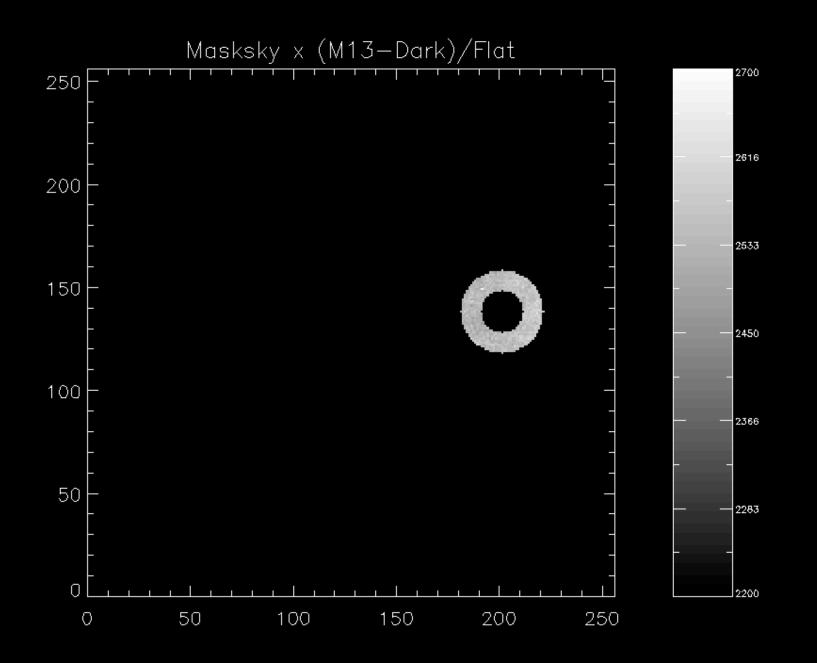












# Computing the Centroid

```
skyval = median( px[wsky] )
print, 'Median sky value = ',skyval
```

; compute the pixel centroids

```
xbar = total(mask*xx * (px-skyval) )/total(mask*(px-
skyval))
ybar = total(mask*yy * (px-skyval))/total(mask*(px-
skyval))
```

```
print,'<x> = ', xbar
print,'<y> = ', ybar
```

# Step 3: Modeling the Noise

- What is the SNR of a given observation?
- How do I choose and optimize the photometric parameters
  - Exposure time required?
  - Aperture diameter?
  - Location and size of sky annuli?

# How to Begin

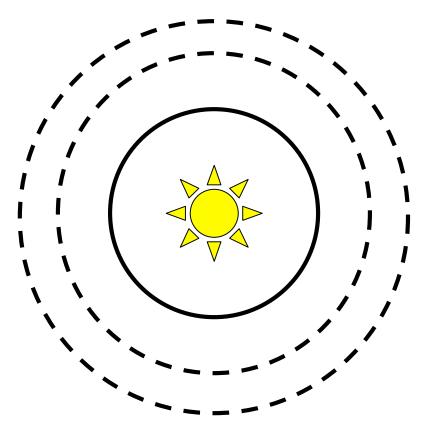
- Write down an expression for the signal and use error propagation to find the noise
  - Express results as signal-to-noise ratio vs. photometric parameters

# The Model

- The purpose is to *estimate* the noise contributions
  - Often getting the answer to within a factor of two is fine
  - Make simplifying assumptions—so long as you can justify them

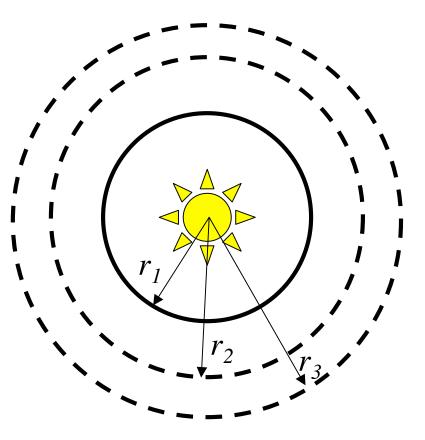
### A Photometric Model

• What parameters describe the measurement?



#### A Photometric Model

- Star
  - Brightness
  - Center  $(x_0, y_0)$
  - Width ( $\sigma$ )
- Sky background in annulus *B*
- Detector
  - QE, readnoise, dark current
- Aperture sizes
  - $-r_1, r_2, r_3$



#### Photometric Model

- Write down an expression for the signal,  $S_i$ , in units of photoelectrons
  - In an individual pixel

$$S_i = F_i + B_i + Q_i + E_i$$

- $F_i$  is the stellar signal =  $f_i t$  at pixel  $i [e^-]$ 
  - Different for every pixel
- $Q_i$  is the dark charge =  $i_i t$  [e<sup>-</sup>] in a given pixel
  - The dark current  $i_i$  varies from pixel to pixel
  - For SNR model assume constant
- $B_i$  is the sky background =  $b_i t$  assumed uniform [e<sup>-</sup>]
  - Varies from pixel to pixel, for SNR model assume constant
- $E_i$  is the readout electronic offset or bias [e<sup>-</sup>]
  - Varies from pixel to pixel, for SNR model assume constant

### The Stellar Signal

• The stellar signal is found by subtracting the background from  $S_i$  and summing over the N pixels that contain the star

$$F_{i} = S_{i} - (B_{i} + Q_{i} + E_{i})$$

$$F_{N} = \sum_{i=1}^{N_{1}} F_{i} = \sum_{i=1}^{N_{1}} S_{i} - (B_{i} + Q_{i} + E_{i})$$

$$N_{1} = \pi r_{1}^{2}$$

- Error in  $F_N$  is due to noise in the signal itself,  $F_N$
- Noise due to dark charge,  $Q_i$
- Noise from the background, *B*
- The read out noise  $\sigma_{RO}$

Noise Sources  

$$F_{N} = \sum_{i=1}^{N_{1}} F_{i} = \sum_{i=1}^{N_{1}} \left[ S_{i} - \underbrace{\left(B_{i} + Q_{i} + E_{i}\right)}_{Background} \right]$$

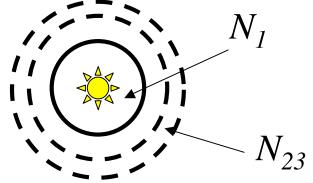
$$\langle B \rangle = \text{ average sky/pixel } \& \langle Q \rangle \text{ the average dark charge/pixel}$$

$$\sigma_{F}^{2} = \underbrace{F_{N}}_{\text{Poisson signalnoise}} + \underbrace{N_{1}\left(\langle B \rangle + \langle Q \rangle + \sigma_{RO}^{2}\right)}_{\text{Poisson noise within } r_{1}} + \underbrace{N_{1}\sigma_{Sky}^{2}}_{\sigma_{Sky}} \text{ is the error in the sky} measured between } r_{2} \& r_{3}$$

$$\sigma_{Sky}^{2} = \left( \langle B \rangle + \langle Q \rangle + \sigma_{RO}^{2} \right) / N_{23}$$

Every pixel between  $r_2 \& r_3$  contributes to the accuracy of the sky measurement

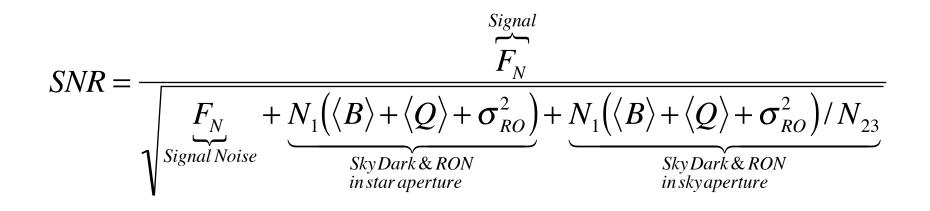
$$\underbrace{N_{1} = \pi r_{1}^{2}}_{Star}, \quad \underbrace{N_{23} = \pi r_{3}^{2} - \pi r_{2}^{2}}_{Sky}$$



# **Noise Sources** $F_{N} = \sum_{i=1}^{N_{1}} F_{i} = \sum_{i=1}^{N_{1}} \left| S_{i} - \underbrace{\left(I_{i} + B_{i} + E_{i}\right)}_{Background} \right|$ $\langle B \rangle$ = average sky/pixel & $\langle Q_d \rangle$ the average dark charge/pixel $\underbrace{F_{N}}_{\text{Poisson signal noise}} + \underbrace{N_{1}\left(\langle B \rangle + \langle Q_{d} \rangle + \sigma_{RO}^{2}\right)}_{\text{Poisson noise within } r_{1}} + \underbrace{N_{1}\left(\langle B \rangle + \langle Q_{d} \rangle + \sigma_{RO}^{2}\right)/N_{23}}_{\text{Poisson noise within } r_{2} < r < r_{3}}$ $\sigma_{F}^{2} =$ $\underbrace{N_{1} = \pi r_{1}^{2}}_{Star}, \quad \underbrace{N_{23} = \pi r_{3}^{2} - \pi r_{2}^{2}}_{Skv}$

- How do we choose  $r_1, r_2, r_3$ ?
  - Signal increases with  $N_1$
  - Noise increases with  $N_1$  and decreases with  $N_{23}$

### Signal-to-Noise



- How do we choose  $r_1, r_2, r_3$ ?
  - Signal increases with  $N_1$
  - Noise increases with  $N_1$  and decreases with  $N_{23}$

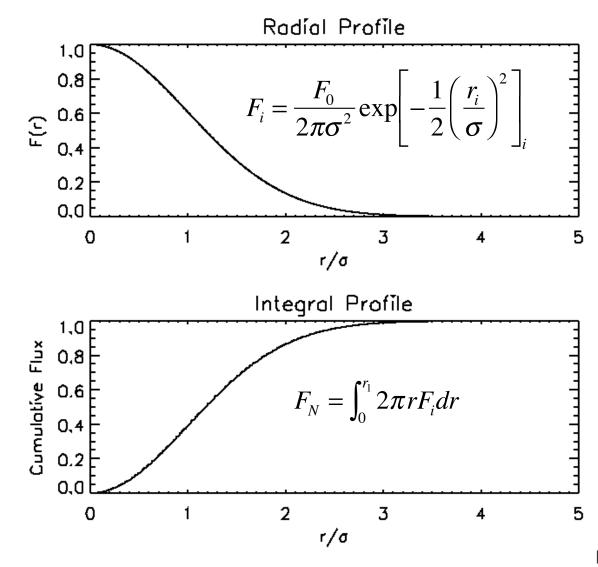
# An Example

• Suppose the stellar signal has a 2-d Gaussian shape

$$F_{i} = \frac{F_{0}}{2\pi\sigma^{2}} \exp\left[-\frac{1}{2}\left(\frac{r_{i}}{\sigma}\right)^{2}\right]_{i}, \quad r_{i}^{2} = (x - x_{0})^{2} + (y - y_{0})^{2}$$
$$F_{N} = \int_{0}^{r_{1}} 2\pi r F_{i} dr$$

– This tells us how  $F_N$  changes with aperture radius

# Star Profile & Integral



11.

# SNR vs. $r_1$

